



Math Virtual Learning

# Probability and Statistics

May 15, 2020



# Probability and Statistics

## Lesson: May 15, 2020

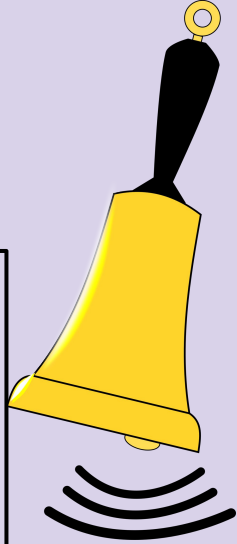
### **Objective/Learning Target:**

Students will be able to find the probability of Compound Events - whether they are an Intersection or Union of events - Day 2

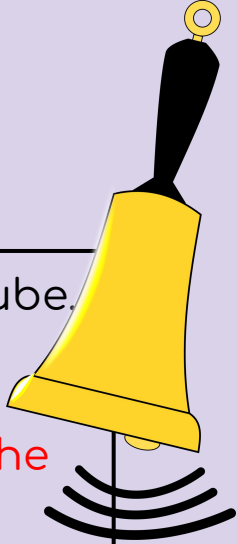
# Let's Get Started!

I am running an experiment where I flip a coin and then roll a number cube.

- What does the notation  $P(H \cup 6)$  mean?
- What does the notation  $P(T \cap \text{Even})$  mean?
- Calculate  $P(H \cup 6)$
- Calculate  $P(T \cap \text{Even})$



# Let's Get Started! ANSWERS



I am running an experiment where I flip a coin and then roll a number cube.

- What does the notation  $P(H \cup 6)$  mean?

This means it is a UNION probability. Therefore we are looking for the chances of flipping a Heads OR rolling a 6.

- What does the notation  $P(T \cap \text{Even})$  mean?

This means it is an INTERSECTION probability. Therefore we are looking for the chances of flipping a Tails AND rolling an even number.

- Calculate  $P(H \cup 6)$

$$P(H) = \frac{1}{2} \quad P(6) = \frac{1}{6} \quad P(H \cup 6) = \frac{1}{2} + \frac{1}{6} = \frac{2}{3}$$

- Calculate  $P(T \cap \text{Even})$

$$P(T) = \frac{1}{2} \quad P(\text{Even}) = \frac{1}{2} \quad P(T \cap \text{Even}) = \frac{1}{2} * \frac{1}{2} = \frac{1}{4}$$

# Practice #1

A card is drawn from a deck of 10 cards numbered 1-10 and a 6 sided die is rolled.

- Would these be Independent or Dependent Events?
- Would this be an Intersection or Union probability?
- Would you add or multiply the probabilities?
- Find the probability of the event



# Practice #1 ANSWER



A card is drawn from a deck of 10 cards numbered 1-10 and a 6 sided die is rolled. Find the probability of drawing card 10 and rolling a 3.

- Would these be Independent or Dependent Events?

**Independent** (cards and dice don't affect each other)

- Would this be an Intersection or Union probability?

**Intersection** (uses "and")

- Would you add or multiply the probabilities? **Multiply**

- Find the probability of the event

$$P(10) = 1/10 \quad P(3) = 1/6 \quad P(10 \cap 6) = 1/10 * 1/6 = 1/60$$

# Practice #2

Jackie has a box of mixed spring flower bulbs containing 12 daffodils, 10 hyacinths, and 14 tulips. Jackie reaches into the box, randomly chooses a bulb, plants it, then chooses another, and plants it. What is the probability that the first bulb Jackie plants is a daffodil and the second is a hyacinth?

- Would these be Independent or Dependent Events?
- Would this be an Intersection or Union probability?
- Would you add or multiply the probabilities?
- Find the probability of the event



## Practice #2 ANSWER

Jackie has a box of mixed spring flower bulbs containing 12 daffodils, 10 hyacinths, and 14 tulips. Jackie reaches into the box, randomly chooses a bulb, plants it, then chooses another, and plants it. What is the probability that the first bulb Jackie plants is a daffodil and the second is a hyacinth?

- Would these be Independent or Dependent Events?

**Dependent (because the 1st bulb is planted and not put back in the box)**

- Would this be an Intersection or Union probability?

**Intersection (because of “and”)**

- Would you add or multiply the probabilities?

**Multiply**

- Find the probability of the event

$$P(D) = 12/36 \quad P(H) = 10/35$$

$$P(D \cap H) = 12/36 * 10/35 = 120/1260 = 2/21$$





## Practice #3

You placed two advertisements in a small 12 page magazine. The ads were placed on pages 3 and 9. What is the probability that, if a customer randomly opens the magazine, he or she will open to a page where your advertisement can be seen?

- Would this be an Intersection or Union probability?
- Would you add or multiply the probabilities?
- Find the probability of the event



# Practice #3 ANSWER

You placed two advertisements in a small 12 page magazine. The ads were placed on pages 3 and 9. What is the probability that, if a customer randomly opens the magazine, he or she will open to a page where your advertisement can be seen?

- Would this be an Intersection or Union probability?

**UNION (because landing on either page will be successful - you don't need both)**

- Would you add or multiply the probabilities?

**Add**

- Find the probability of the event

$$P(\text{page 3}) = 1/12 \quad P(\text{page 9}) = 1/12$$

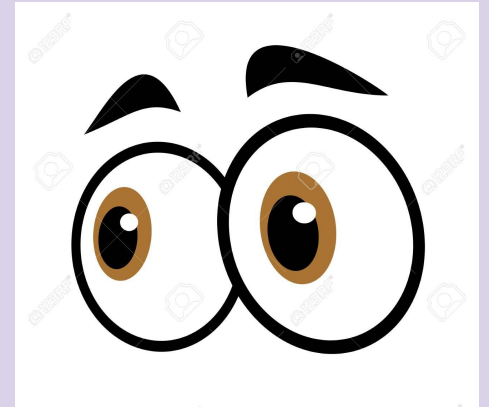
$$P(3 \cup 6) = 1/12 + 1/12 = 2/12 = 1/6$$



# Practice #4

In a group of 92 students, 40 have brown eyes and 35 have hazel eyes. 20 students have both brown eyes and blue eyes. Find the probability that a student picked from this group at random either has hazel or brown eyes.

- Would this be an Intersection or Union probability?
- Would you add or multiply the probabilities?
- Find the probability of the event



## Practice #4 ANSWER

In a group of 92 students, 40 have brown eyes and 35 have hazel eyes. 20 students have both brown eyes and blue eyes. Find the probability that a student picked from this group at random either has hazel or brown eyes.

- Would this be an Intersection or Union probability?

**Union (because of the words “either/or”)**

- Would you add or multiply the probabilities? **ADD**
- Find the probability of the event

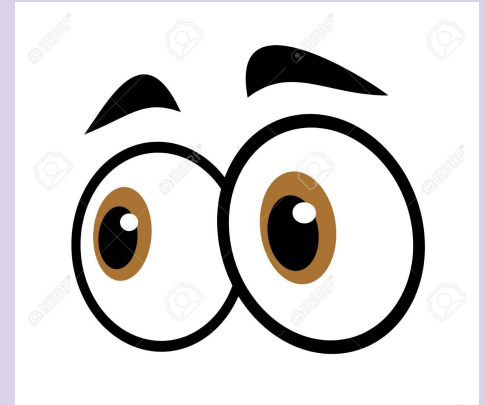
$$P(\text{Brown Eyes}) = 40/92$$

$$P(\text{Blue Eyes}) = 35/92$$

$$P(\text{Brown U Blue}) = 40/92 + 35/92 = 75/92$$

**BUT - 20 of those had both and were counted twice so we need to take that double count out**

$$75 - 20 = 55 \dots P(\text{Brown U Blue}) = 55/92$$



## Practice #5

A box of fruit contains 5 oranges, 3 bananas, 6 plums and 2 apples. James is packing his lunch and will include 2 pieces of fruit. What is the probability that he will randomly pick an apple and then a banana?

- Would these be Independent or Dependent Events?
- Would this be an Intersection or Union probability?
- Would you add or multiply the probabilities?
- Find the probability of the event



# Practice #5 ANSWER

A box of fruit contains 5 oranges, 3 bananas, 6 plums and 2 apples. James is packing his lunch and will include 2 pieces of fruit. What is the probability that he will randomly pick an apple and then a banana?

- Would these be Independent or Dependent Events?

**Dependent** (because the 1st piece of fruit is packed into the lunch & not put back in the box)

- Would this be an Intersection or Union probability?

**Intersection** (because of “and”)

- Would you add or multiply the probabilities?

**Multiply**

- Find the probability of the event

$$P(A) = 2/16 \quad P(B) = 3/16$$

$$P(A \cap B) = 2/16 * 3/16 = 6/256 = 3/128$$



## Practice #6

A local charity is hosting a fundraiser. When you purchased your entry ticket it was printed on red paper with the number 10 in the corner. Upon arrival you realized that the fundraiser is giving away a cruise. They will spin the spinner below and then draw a number between 1 and 30 out of a hat. If the color and number match your ticket, you win a cruise. What is the probability that you will win?

- Would these be Independent or Dependent Events?
- Would this be an Intersection or Union probability?
- Would you add or multiply the probabilities?
- Find the probability of the event



# Practice #6 ANSWER

A local charity is hosting a fundraiser. When you purchased your entry ticket it was printed on red paper with the number 10 in the corner. Upon arrival you realized that the fundraiser is giving away a cruise. They will spin the spinner below and then draw a number between 1 and 30 out of a hat. If the color and number match your ticket, you win a cruise. What is the probability that you will win?

- Would these be Independent or Dependent Events?

**Independent** (because the the spinner and hat of numbers are two separate things)

- Would this be an Intersection or Union probability?

**Intersection** (because of “and”)

- Would you add or multiply the probabilities?

**Multiply**

- Find the probability of the event

$$P(R) = 1/6 \quad P(10) = 1/30$$

$$P(A \cap B) = 1/6 * 1/30 = 1/180 = 0.5\% \text{ of winning}$$





## Practice #7

The letters to the word PROBABILITY were cut up and put into a bag. Three of the letters will be drawn at random and not replaced into the bag. What is the probability that the letters drawn in order will spell BAT?

- Would these be Independent or Dependent Events?
- Would this be an Intersection or Union probability?
- Would you add or multiply the probabilities?
- Find the probability of the event



# Practice #7 ANSWER

The letters to the word PROBABILITY were cut up and put into a bag. Three of the letters will be drawn at random and not replaced into the bag. What is the probability that the letters drawn in order will spell BAT?

- Would these be Independent or Dependent Events?

**Dependent** (because the letters are not replaced after being drawn)

- Would this be an Intersection or Union probability?

**Intersection** (because the order has to be B and then A and then T)

- Would you add or multiply the probabilities?

**Multiply**

- Find the probability of the event

$$P(B) = 2/11$$

$$P(A) = 1/10$$

$$P(T) = 1/9$$

$$P(B \cap A \cap T) = 2/11 * 1/10 * 1/9 = 2/990 = 0.2\% \text{ of spelling BAT}$$



# Practice #8

In a group of 100 people, 19 were drinking punch and 23 were eating goldfish crackers. None of the people were eating both. Find the probability that a person picked from this group at random is either drinking punch or eating goldfish.

- Would this be an Intersection or Union probability?
- Would you add or multiply the probabilities?
- Find the probability of the event



# Practice #8

In a group of 100 people, 19 were drinking punch and 23 were eating goldfish crackers. None of the people were eating both. Find the probability that a person picked from this group at random is either drinking punch or eating goldfish.

- Would this be an Intersection or Union probability?

**UNION because of the “or”**

- Would you add or multiply the probabilities? **ADD**
- Find the probability of the event

$$19/100 + 23/100 = 42/100 = 21/50$$

